Exciton coherence in semiconductor quantum dots

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Received 17 June 2008, revised 25 July 2008, accepted 30 July 2008
Published online 30 September 2008

PACS 71.35.-y, 78.47.jf, 78.47.nj, 78.67.Hc

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The coherent dynamics of excitons in InAs quantum dots (QDs) was investigated in the telecommunication wavelength range using a transient four-wave mixing technique. The sample was fabricated on an InP(311)B substrate using strain compensation to control the emission wavelength. This technique also enabled us to fabricate a 150-layer stacked QD structure for obtaining a high S/N in the four-wave mixing measurements, although no high-sensitive heterodyne detection was carried out. The dephasing time and transition dipole moment were precisely estimated from the polarization dependence of signals, taking into account their anisotropic properties.

1 Introduction The coherent dynamics and manipulation of excitons in self-assembled quantum dots (SAQDs) have been key issues in the implementation of quantum information processing and quantum communications [1, 2]. SAQDs that emit light at telecommunication wavelengths have attracted significant interest because of their possible applications in long-distance optical [3] and quantum communications [4, 5]. Hence, fabrication techniques such as strain compensation [5–7] and the double-cap method [7, 8] have been developed to redshift the emission wavelength of SAQDs. Recently, some research groups have reported the advantages of strain-compensated InAs SAQDs grown on an InP(311)B substrate [6, 7, 9, 10]. These advantages include long-wavelength emission and realization of a multilayer stacked structure without defects and imperfections. Owing to the orientation of (311)B substrates, SAQDs grown on an InP(311)B substrate should exhibit optical anisotropy, which is analogous to that exhibited for quantum wells grown on a (311)B substrate [11]. Optical anisotropy is expected to affect the coherent and population dynamics of excitons. For investigating these dynamics, we must perform polarization-sensitive transient nonlinear spectroscopies, such as four-wave mixing (FWM) and pump-probe (PP) spectroscopies, under resonant excitation of the exciton ground states. However, it is difficult to apply these techniques to QDs when the signal intensity is weak owing to a low QD density. Hence, to enhance the nonlinear signals, we used a multilayer stacked structure of strain-compensated SAQDs to enhance nonlinear signals [12, 13].

In this paper, we report the investigation of the coherent and population dynamics of excitons using transient FWM and PP spectroscopic techniques under resonant excitation in the telecommunication wavelength range. InAs
SAQDs grown on an InP(311)B substrate using strain compensation were used as the sample. Polarization-sensitive measurements enabled us to estimate the individual exciton lifetimes and dephasing times for two orthogonally polarized exciton ground states. Hence, the exciton ground states of our QDs are split into orthogonally polarized states in the [011] (x) and [233] (y) direction. In this study, we use |x⟩ and |y⟩ to represent the x— and y—polarized states, respectively.

The time evolution of exciton coherence and population was measured using transient FWM and PP techniques. All the measurements were performed using 1.1-ps optical pulses (repetition rate: 76 MHz) generated from an optical parametric oscillator pumped by a mode-locked Ti:sapphire laser. The dashed line in Fig. 1(c) indicates the spectrum of the incident pulses. The wavelength of the incident pulses was tuned to 1.468 μm to excite the ground-state excitons resonantly. The polarization directions of the linearly polarized incident pulses were controlled using half-wave plates to investigate the polarization dependences of the FWM and PP signals. The polarization selection rules allowed us to selectively excite either the |x⟩ or |y⟩ states. In this paper, the angle between the polarization direction of the incident pulses and the [011] direction is represented as θ. The sample was maintained at 3 K for all the measurements.

The FWM experiment was performed using the two-pulse self-diffraction configuration to measure the dephasing time T2 of excitons. A schematic image of the experimental setup is shown in the inset of Fig. 2(a). The time-integrated FWM signal intensity in the 2k2 − k1 direction was measured as a function of the time delay τ between two excitation pulses. The k1 and k2 pulses had parallel polarizations. The intensities of the excitation pulses were adjusted to 16 kW/cm²; at this intensity, no significant excitation dependence of T2 was observed. A PP experiment was performed in the transmission geometry to investigate the population dynamics of the excitons. The differential transmission (DT) of the probe pulse was detected for various τ values between the pump and probe pulses. The in-
tensity of the pump pulse was the same as that used in the FWM experiment, and the intensity of the probe pulse was 0.5% of that of the pump pulse.

3 Results and discussion

3.1 Four-wave mixing spectroscopy  Figure 2(a) shows typical FWM signals for various polarization directions, θ. At τ < 60 ps, a beat signal was observed only for θ = 45°, where the |x⟩ and |y⟩ states were simultaneously excited. Thus, the beat signal resulted from the coherent superposition between the x− and the y−polarized transitions. This is well known as a fine-structure quantum beat [16]. The period of the beat was estimated to be 23 ps, which corresponds to a splitting energy of 180 μeV. The quantum beat almost vanished for θ = 0° and 90°. This clearly proves the polarization selection rules with respect to |0⟩ − |x⟩ and |0⟩ − |y⟩ transitions.

For a long τ, the observed FWM signal decayed exponentially with a large time constant, indicating the long dephasing time of the excitons in the QDs. The decay time constants and signal intensities of the slow component were clearly different for x− and y−polarizations. The anisotropy of the decay time indicates that the T2 values for the x− and y−polarized transitions significantly differ from each other. We estimated the T2 values to be T2^x = 2.86 ns for the x−polarized transition and T2^y = 1.64 ns for the y−polarized transition [13]. The T2^x value is larger than any other T2 value reported for QD excitons so far [1, 17–20]. Using the equation γ = 2ℏ/γ, we calculated the homogeneous broadenings of the zero-phonon lines γ to be γ^x = 0.46 ± 0.01 μeV and γ^y = 0.80 ± 0.01 μeV.

The polarization dependence of the FWM signal intensity is related to the anisotropy of the transition dipole moment |μ| for the x− and y−polarized transitions because an FWM signal intensity is proportional to |μ|^2. Figure 2(b) shows the FWM intensities for τ = 200 ps measured in various polarization directions, θ, of the incident pulses at the same incident intensities. In general, an FWM intensity is proportional to E^0|μ|^2 exp(−4τ/T^z) + |μ|^2 SIN^2θ exp(−4τ/T^y)). The theoretical curve calculated by the equation is in excellent agreement with the experimental data shown in Fig. 2(b). In the calculation, we used the values of T^x and T^y estimated from the decay time constants of the FWM intensity. Consequently, the ratio of |μ|^2 for x− and y−polarized transitions was estimated to be |μ|^2/|μ|^2 = 1.72 ± 0.04.

This ratio coincides with the ratio of T^x/T^y = 1.75 ± 0.07. This agreement implies that T^x are dominantly by the radiative lifetimes, T^x, because T^y is proportional to |μ|^2. In other words, all dephasing due to non-radiative population relaxation and pure dephasing without population relaxation are very small [19]. A similar analysis was performed by W. Langbein et al. They also found a radiatively limited T^x in InAs/GaAs QDs grown on a GaAs(100) substrate at shorter wavelengths [19] compared to that used in this study. Table 1 shows the comparison of T^x and other parameters obtained for the QDs investigated by W. Lang-
bein et al. using the polarization-dependent FWM method with those of our QDs. We found that the $T_2^\parallel$ for our QDs is longer than that for their QDs, while the $T_2^\perp$'s are similar in both cases. This is due to the large anisotropy of $|\mu|$ in our QDs. One of the possible origins of the large anisotropy is the low symmetry of the high-index substrate [15]. Our result demonstrates that substrate orientation is one of effective factors that determine the anisotropy of $|\mu|$, i.e., a radiatively limited $T_2$.

Table 1 Dephasing time $T_2$ and other parameters for strain-compensated InAs QDs obtained from FWM measurements. For comparison, parameters of InAs QDs reported by W. Langbein et al. are summarized.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Present work</th>
<th>Langbein’s work [19]</th>
</tr>
</thead>
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<td>QD/spacer</td>
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<td>InAs/GaAs</td>
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<tr>
<td>substrate</td>
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<td>GaAs(100)</td>
</tr>
<tr>
<td>wavelength</td>
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<td></td>
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<tr>
<td>$T_2^\parallel$ (temp.)</td>
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<td>2.1 ns (5 K)</td>
</tr>
<tr>
<td>$T_2^\perp$ (temp.)</td>
<td>1.64 ns (3 K)</td>
<td>1.6 ns (5 K)</td>
</tr>
<tr>
<td>$T_2^\parallel/T_2^\perp$</td>
<td>1.75 ± 0.07</td>
<td>1.316 ± 0.005</td>
</tr>
<tr>
<td>$</td>
<td>\mu^x/</td>
<td>\mu^y</td>
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</tbody>
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3.2 Pump-probe spectroscopy For a more precise estimation of the radiative contribution to dephasing, we measured the absolute value of $T_r$ by using a polarization-dependent PP technique. The time evolution of DT is determined only by the population dynamics of the excitons because we could ignore the effect of biexciton formation due to the narrow band and the weakness of the pump pulse. To analyse the DT decay rates, we considered the relaxation times shown in Fig. 3. $T_r^{(x)}$ and $T_r^{(y)}$ represents the population decay times due to the radiative and non-radiative transitions from the $|x\rangle$ ($|y\rangle$) state to $|0\rangle$ state. $T_{nr}^{(x)}$ represents the polarization relaxation time between $|x\rangle$ and $|y\rangle$.

Figure 4(a) shows the DT at various $\tau$ for the $x$ and $y$ polarizations of the pump pulse. Adhering to the polarization selection rules, we selectively excited the exciton ground state that had the same polarization as the pump pulse at zero delay. The probe pulses were cross-linearly polarized with respect to the pump pulses. The DT profiles were well fitted by single exponential functions with different decay time constants. The DT decay times were determined to be $t^x = 1.7$ ns and $t^y = 1.0$ ns, which are clearly anisotropic.

The DT decay time is generally influenced not only by $T_r^{(x)}$ but also by $T_{nr}^{(x)}$ and $T_{nr}^{(y)}$. To simplify the analysis of the experimental results, we independently estimated $T_{nr}^{(y)}$ by measuring the polarization degree. Figure 4(b) shows the time evolution of the polarization degree when the $y$-polarized state is selectively excited by the pump pulse. The polarization degree did not change for $\tau < 1.5$ ns. From the exponential fitting of the polarization degree, $T_{nr}^{(y)}$ was found to be at least longer than several tens of nanoseconds. The value of $T_{nr}^{(y)}$ is considerably longer than the typical value of $T_r$, which is of the order of 1 ns. Therefore, the contribution of the polarization relaxation to the DT decay rates observed in Fig. 4(a) is negligible. In this case, the DT decay time in Fig. 4(a) is determined by $T_r^{(x)}$ and $T_{nr}^{(y)}$ of the exciton ground state that is selectively excited by the pump pulse. Since $T_r$ is proportional to $|\mu|^{-2}$, the ratio $T_r^{(x)}/T_r^{(y)}$ should be $|\mu^x/|\mu^y|^2$.

The ratio $t^x/t^y = 1.7 \pm 0.2$ is in quantitative agreement with the ratio $|\mu^x/|\mu^y|^2$ estimated in the FWM measurements, within a margin of error. Therefore, the DT decay time should directly correspond to $T_r$, and for our QDs, the non-radiative population relaxation was found to be negligible compared with the radiative population relaxations. Thus, we conclude that $T_r = 1.7$ ns and $T_r = 1.0$ ns. This result clearly demonstrates the high crystalline nature of our QDs. This is one of the reasons why our QDs show a long $T_2$.

![Figure 3](https://example.com/figure3.png)

**Figure 3** Energy-level diagram and optically allowed transitions related to exciton ground states in QD with broken rotational invariance. $|x\rangle$ and $|y\rangle$ correspond to the $x$- and $y$-polarized states. The parameters in the diagram represent the relaxation times, as explained in the text.

The precise measurement of $T_r$ enabled us to calculate the absolute value of $|\mu|$. $|\mu|^2$ can be determined using the equation [22]

$$|\mu|^2 = \left[ \frac{9e^{5/2}}{(2c + \epsilon_{QD})^2 \pi \epsilon_0 \hbar \omega_0^3} \right]^{-1} \frac{1}{T_r},$$

where $\epsilon_{QD}$ and $c$ represent the dielectric constant for the QDs and their surrounding medium, respectively. The calculated values of $|\mu|^2$ are $|\mu^x|^2 = 45$ Debye and $|\mu^y|^2 = 58$ Debye. These values are larger than those reported for In(Ga)As SAQDs; that is, excitons in our SAQDs strongly interact with light. The values of $|\mu|^2$ were also found to be in good agreement with those estimated from the Rabi frequency, including their anisotropic characteristics [23].
This agreement demonstrates the high precision of the values of $T_\pi$ measured by PP spectroscopy.

3.3 Precise estimation of pure dephasing The simultaneous measurement of the FWM and PP signals enabled us to estimate pure dephasing, $\gamma_{\text{pure}}$, which causes dephasing without changing the exciton population. The relationship between $\gamma_h$, $\gamma_r$, and $\gamma_{\text{pure}}$ is expressed by the equation $\gamma_h = \gamma_r + \gamma_{\text{pure}}$ when the non-radiative population relaxation is negligible, as described in the previous subsection. $\gamma_r$ represents the dephasing caused by the radiative population relaxation. From the results of PP spectroscopy, we calculated the radiative dephasing to be $\gamma_r = 0.38 \pm 0.01 \mu$eV and $\gamma_r' = 0.65 \pm 0.06 \mu$eV using the relation $\gamma_r = h/T_\pi$. These values are very close to those of $\gamma_h$. This confirms the conclusions made in the previous subsections, i.e. the dephasing is mainly caused by the radiative recombination process, and the pure dephasing is very small. By comparing $\gamma_r$ with $\gamma_r'$, we estimated the values of $\gamma_{\text{pure}}$ to be $\gamma_{\text{pure}} = 0.08 \pm 0.02 \mu$eV and $\gamma_{\text{pure}}' = 0.15 \pm 0.07 \mu$eV. Thus, the obtained $\gamma_{\text{pure}}$ is considerably smaller than the typical values for QDs reported in previous studies.

The error in the estimation of $\gamma_{\text{pure}}$ is greater than 0.1 $\mu$eV, as described above, though the excitation intensity was weak and no high-sensitive heterodyne detection was performed. The estimation error is significantly smaller than that reported in earlier studies since in our FWM and PP measurements, we could achieve a high signal-to-noise ratio (S/N) by using a 150-layer-stacked structure of QDs [12]. Moreover, the simultaneous measurement of the FWM and PP signals with a high S/N afforded a greater accuracy in the determination of $\gamma_{\text{pure}}$ than did the measurement of the FWM signals alone. The highly accurate measurement of $\gamma_{\text{pure}}$ greatly assists the investigation of a pure dephasing mechanism, such as exciton-phonon interactions, which still remains a critical issue in physics of QDs. Temperature-dependent measurements of $\gamma_{\text{pure}}$ will provide a detailed information on the pure dephasing mechanism, which will be published elsewhere.

4 Conclusions We performed transient FWM and PP spectroscopies to investigate the coherent and population dynamics of excitons in strain-compensated InAs SAQDs grown on an InP(311)B substrate. The emission wavelength of an exciton ground state was in the telecommunication wavelength range. The radiative lifetime and dephasing time exhibited large in-plane anisotropy due to the anisotropy of the transition dipole moment. The anisotropy of our QDs is larger than that of the QDs grown on a GaAs(100) substrate, which is due to the low symmetry of the high-index substrate employed in this study. The polarization dependence of the decay times of both the FWM and the PP signals is in quantitative agreement with the polarization dependence of the transition dipole moment. This shows that non-radiative population relaxation, polarization relaxation and pure dephasing are considerably smaller than radiative population relaxation. These results clearly indicate that our strain-compensated QDs have excellent optical properties. The simultaneous measurements of the FWM and PP signals with a high signal-to-noise ratio allowed us to directly measure the pure dephasing with an accuracy of greater than 0.1 $\mu$eV, which gives a powerful tool to investigate pure dephasing mechanism in QDs.

Acknowledgements This study was partially supported by a Grant-in-Aid for Scientific Research from the Ministry of Education, Culture, Sports, Science, and Technology of Japan. All the samples were fabricated at the Photonic Device Laboratory, NICT.

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